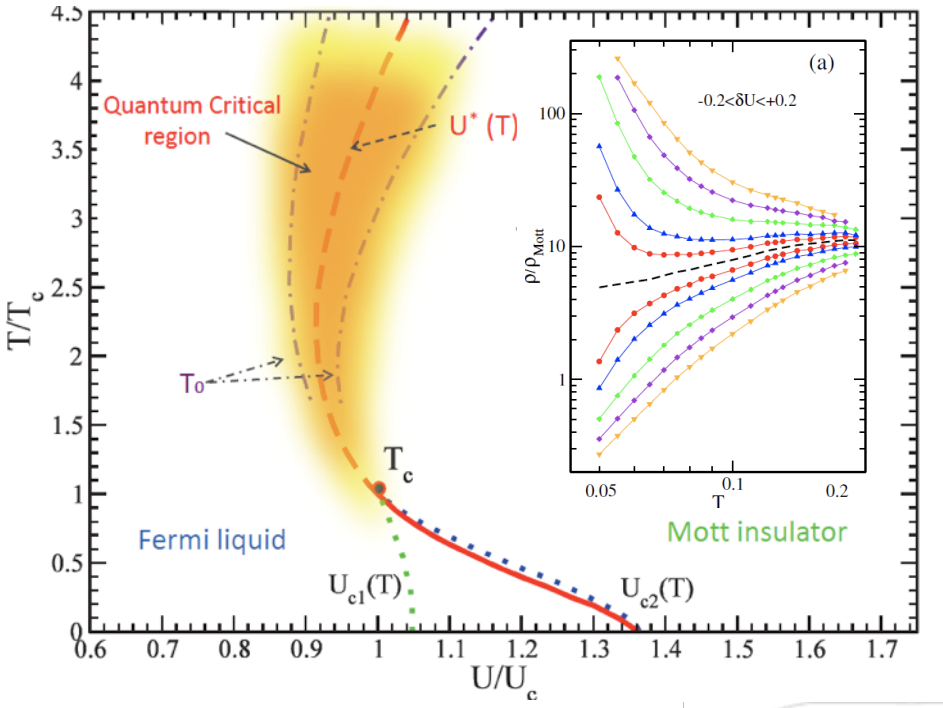
Quantum Critical Behavior at the Mott Point

Vladimir Dobrosavljevic
Florida State University

http://badmetals.magnet.fsu.edu

NATIONAL HIGH MAGNETIC FIELD LAB



Collaborators:

Hanna Terletska *(FSU, Michigan)*
Jaksa Vucicevic *(Belgrade, Saclay)*
Darko Tanaskovic *(Belgrade)*
Marcelo Rozenberg *(Orsay)*

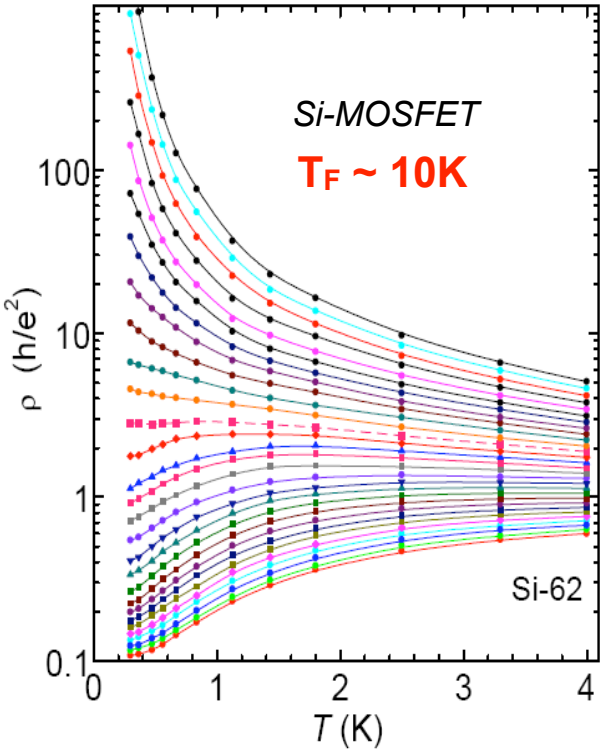
Abrahams, Chakravarty, Kotliar, Haule, Miranda, Pankov,...

Funding: ***NSF grants:***
DMR-1410132
…

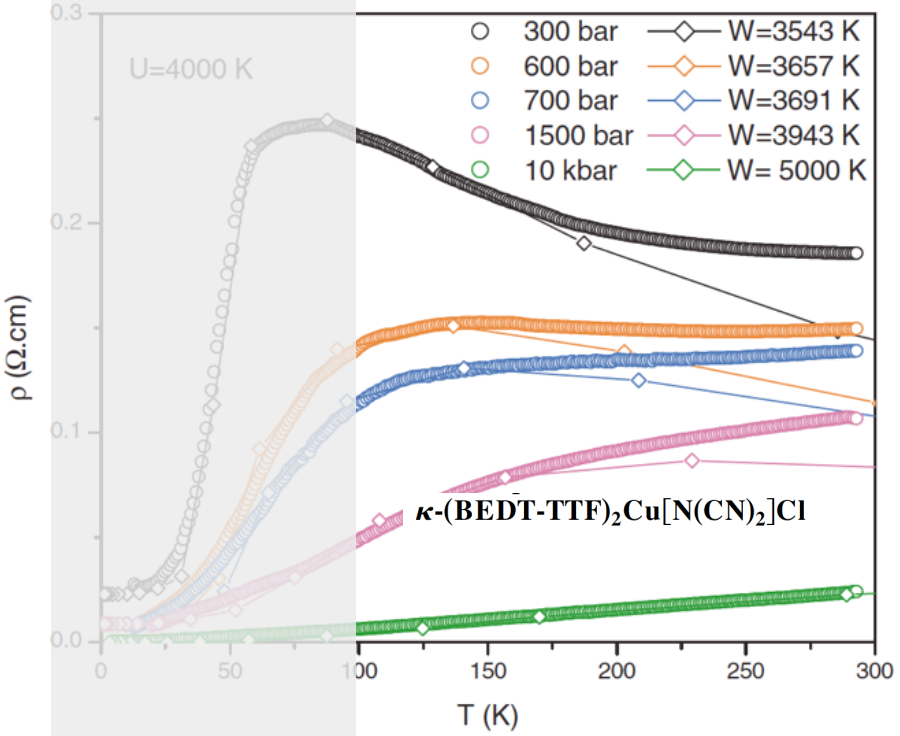
From Metals to Insulators:

universality at ``high temperatures”

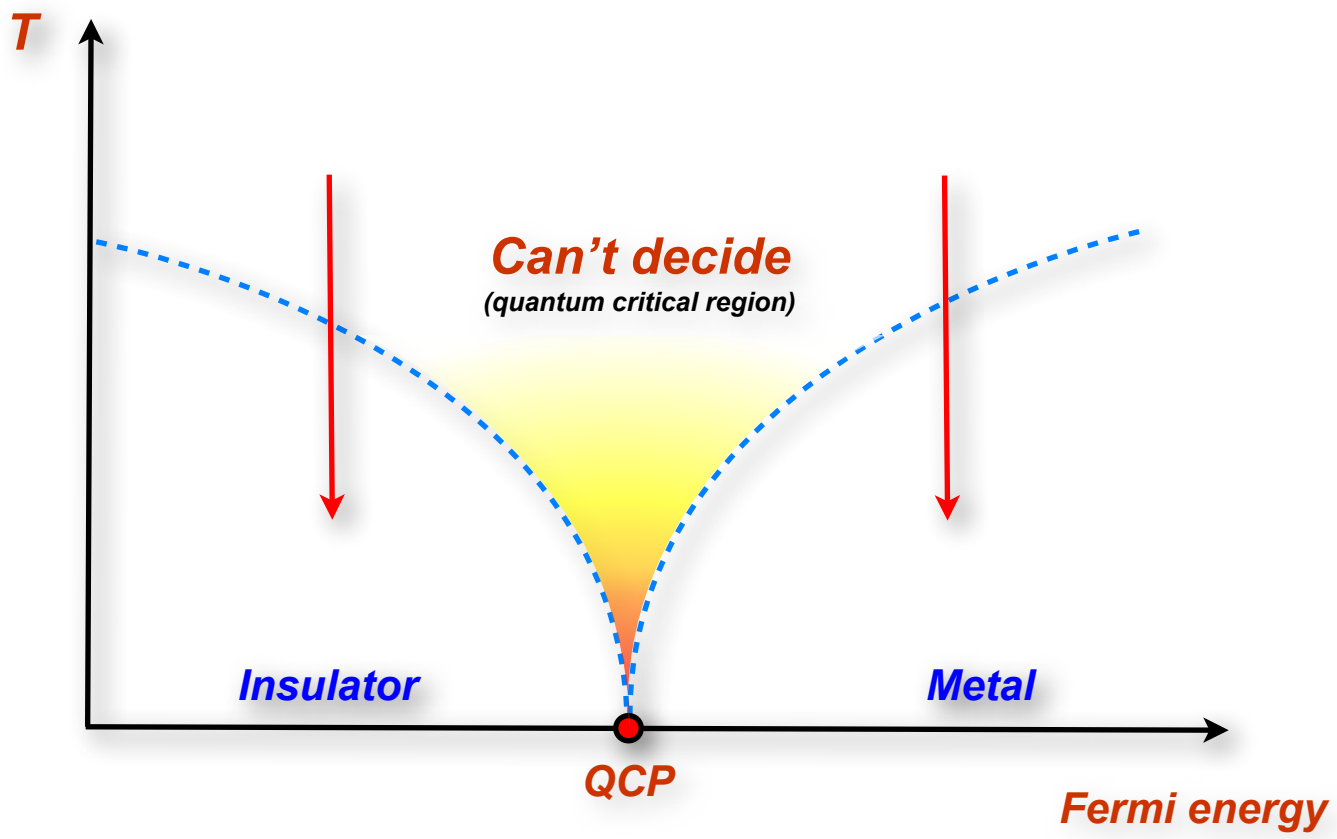
carrier density: Wigner-Mott 2DEG



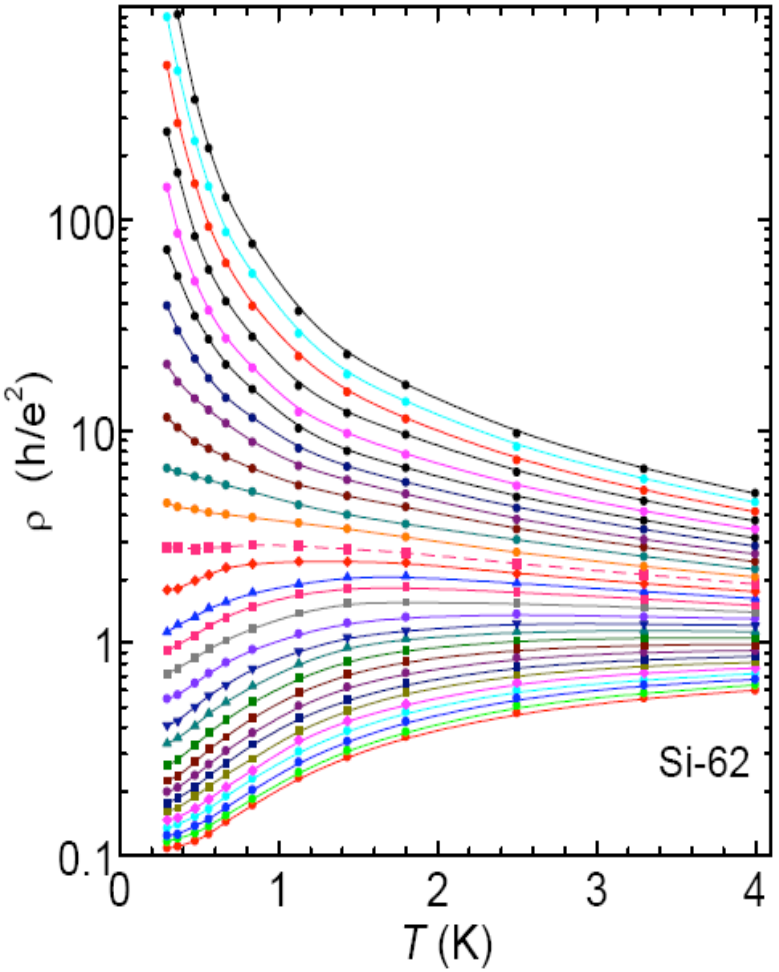
pressure: Mott organics

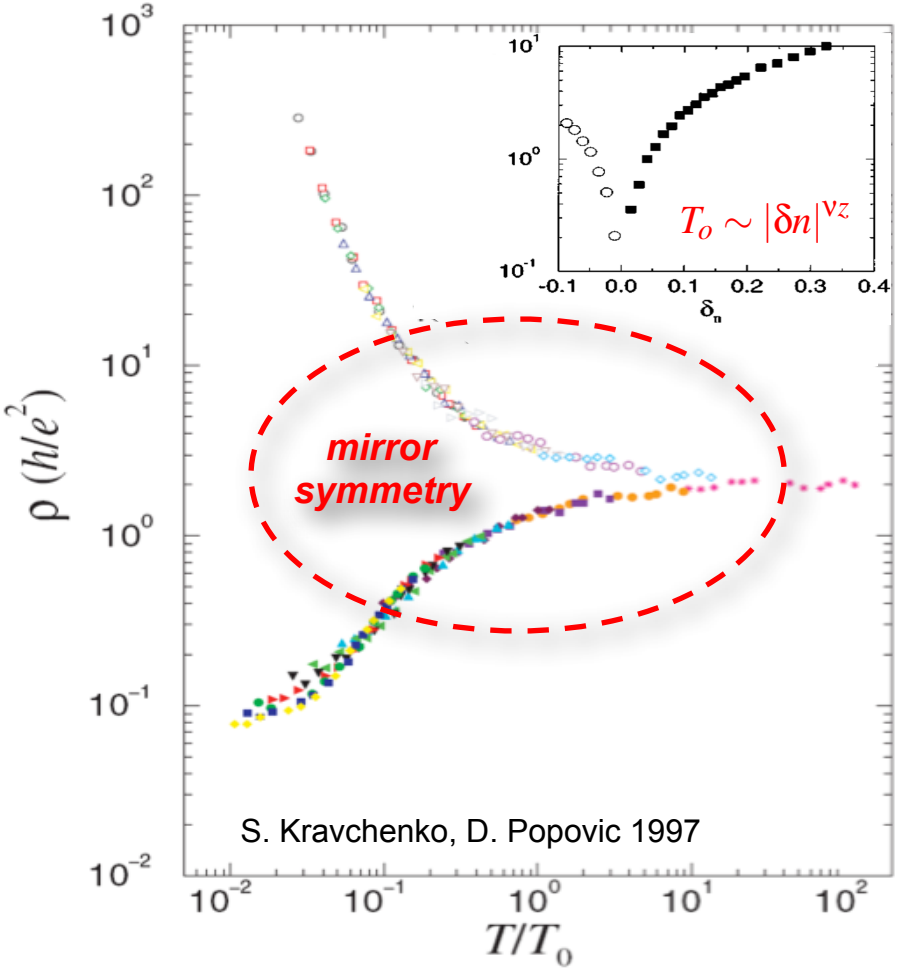


MIT Quantum Criticality?



2D-MIT: “Duality” Scaling???





Scaling Theory Redux

VOLUME 79, NUMBER 3 PHYSICAL REVIEW LETTERS 21 JULY 1997

Scaling Theory of Two-Dimensional Metal-Insulator Transitions

V. Dobrosavljević,[1] Elihu Abrahams,[1,2] E. Miranda,[1] and Sudip Chakravarty[3]
[1]*National High Magnetic Field Laboratory, Florida State University 1800 E. Paul Dirac Drive, Tallahassee, Florida 32306*
[2]*Serin Physics Laboratory, Rutgers University, Piscataway, New Jersey 08855-0849*
[3]*Department of Physics and Astronomy, University of California Los Angeles, Los Angeles, California 90095-1547*
(Received 10 April 1997)

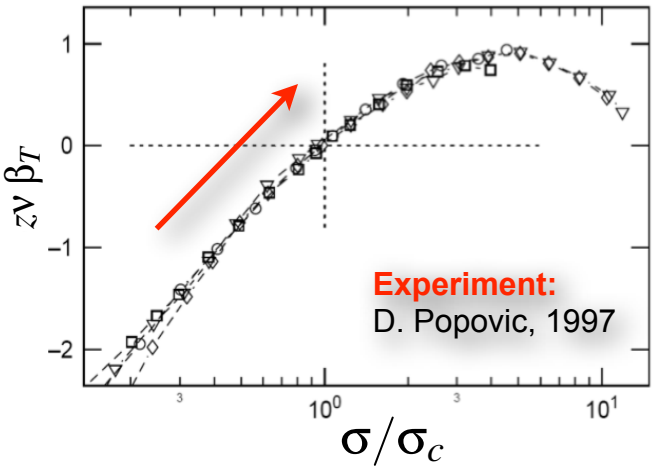
We discuss the recently discovered two-dimensional metal-insulator transition in zero magnetic field in the light of the scaling theory of localization. We demonstrate that the observed symmetry relating conductivity and resistivity follows directly from the quantum critical behavior associated with such a

"strong coupling" - dominated by insulator?

$$\beta_T(g) = -\frac{d\ln g}{d\ln T} \approx \frac{1}{\nu z}\ln g$$

$$g(T) \approx g_o \exp\{\delta n (T_o/T)^{1/\nu z}\}$$

$$g^*(\delta n, T = 1/g^*(-\delta n, T)$$



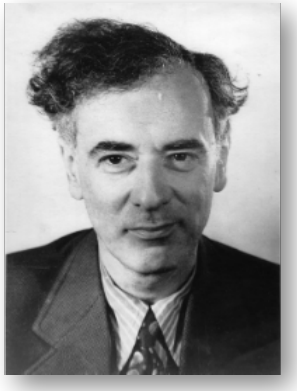
How to tackle Phase Transitions?

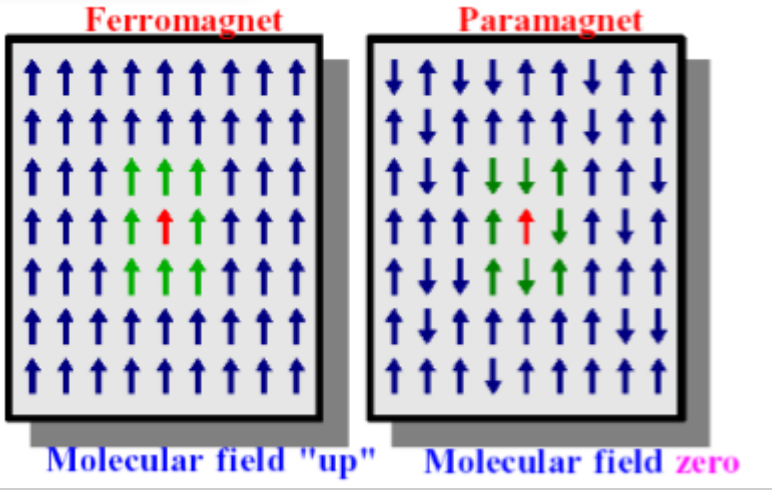
Standard critical points:

Spontaneous symmetry breaking

Order parameter, Landau-Ginzburg

Renormalization group, field theory



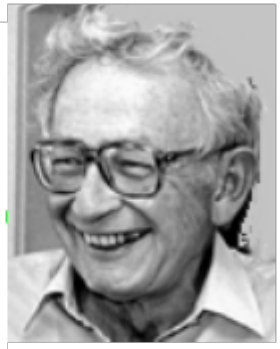


Metal-Insulator Transitions:

NO symmetry breaking!

Order parameter???

"...orthodox phase transition theory will be of little help to us for the time being, and thus the great body of literature in the field is simply irrelevant..."
Ill–Condensed Matter, 1979



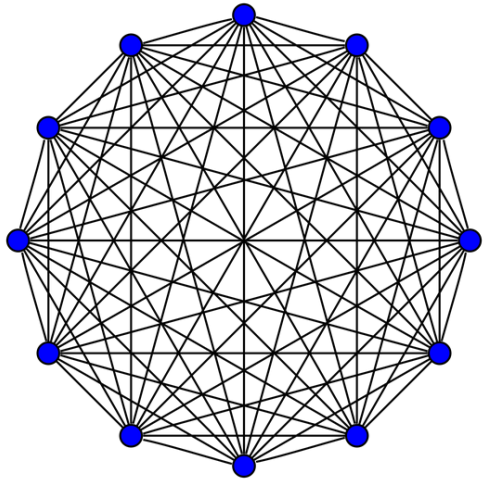
Phillip W. Anderson

Maximally Frustrated Hubbard Model

$$H = -t \sum_{\langle i,j \rangle, \sigma} \left(c^{\dagger}_{i\sigma} c_{j\sigma} + \text{h.c.} \right) + U \sum_{i} n_{i\uparrow} n_{i\downarrow} - \mu \sum_{i,\sigma} c^{\dagger}_{i\sigma} c_{i\sigma}$$

1992

Gabi Kotliar



Infinite-range model

Suppress all orders: “pure Mott”

Local self-energy: DMFT solution

“Kondo physics” forms Fermi liquid

Finite temperature transport: the Mott transition at half-filling

PRL 107, 026401 (2011) PHYSICAL REVIEW LETTERS week ending 8 JULY 2011

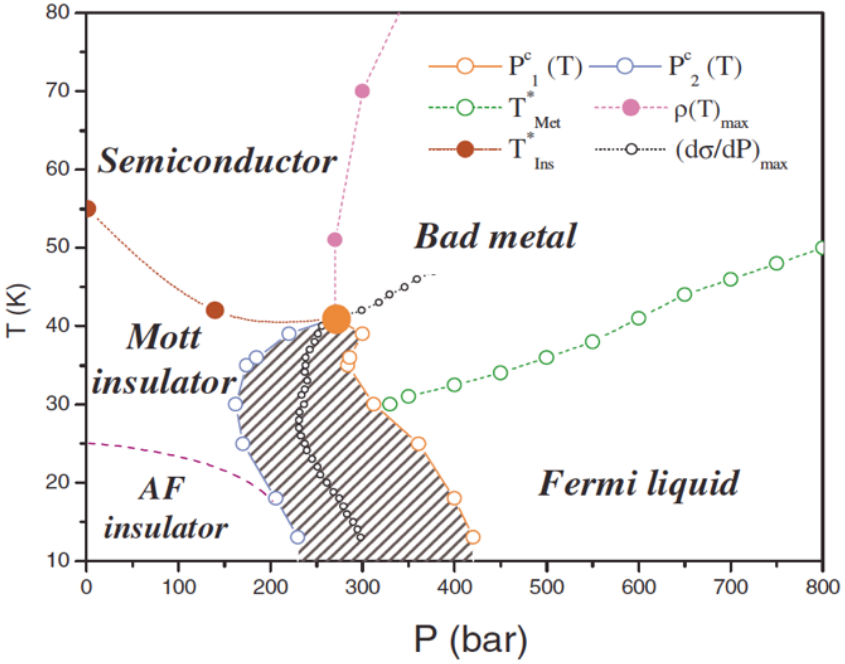
Quantum Critical Transport near the Mott Transition

H. Terletska,[1] J. Vučičević,[2] D. Tanasković,[2] and V. Dobrosavljević[1]

(also J. Vučičevic, et al., Phys. Rev. B, 88, 075143 (2013))

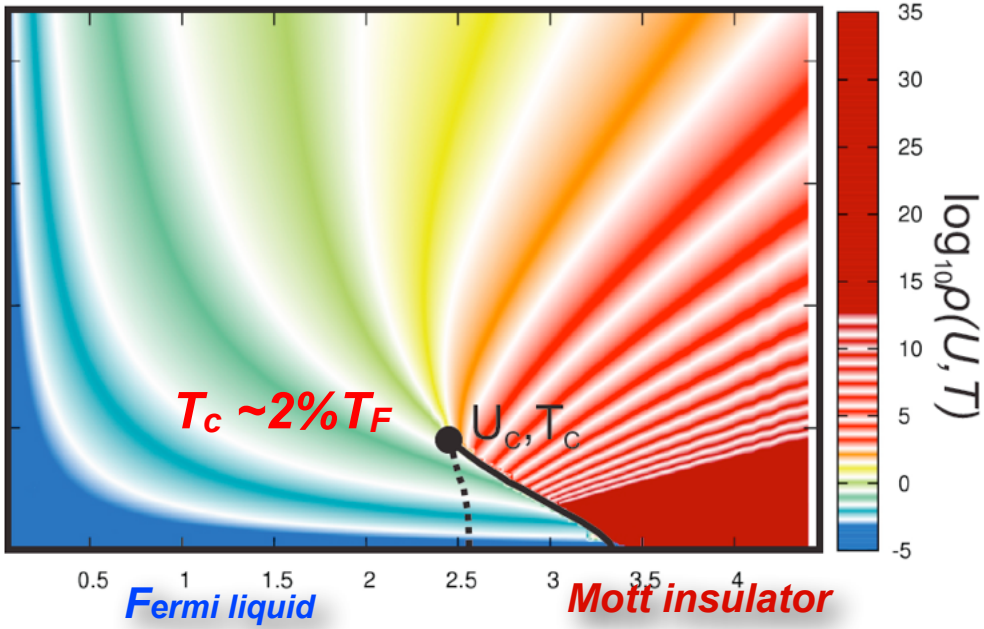
Experiment: organic Mott system

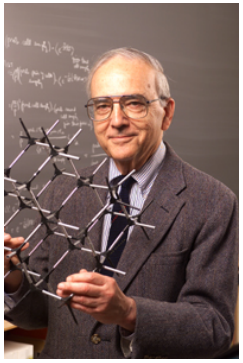
Jerome, PRL 2003



Theory (DMFT)

Early work: Kotliar, Rozenberg 1992, etc.



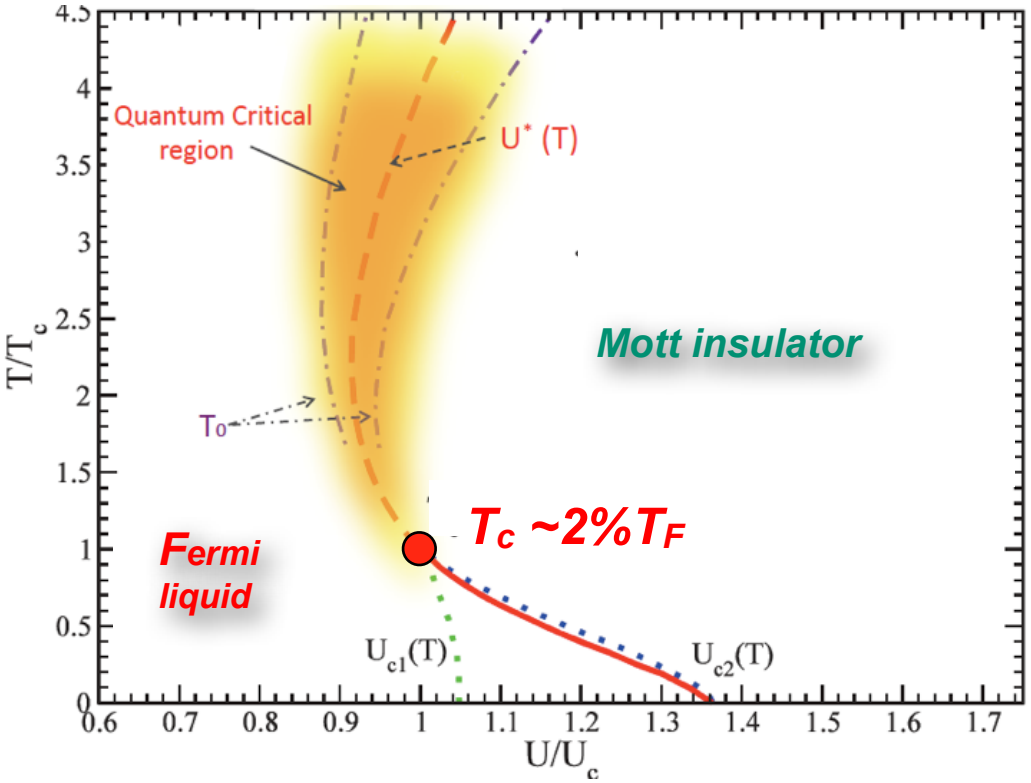


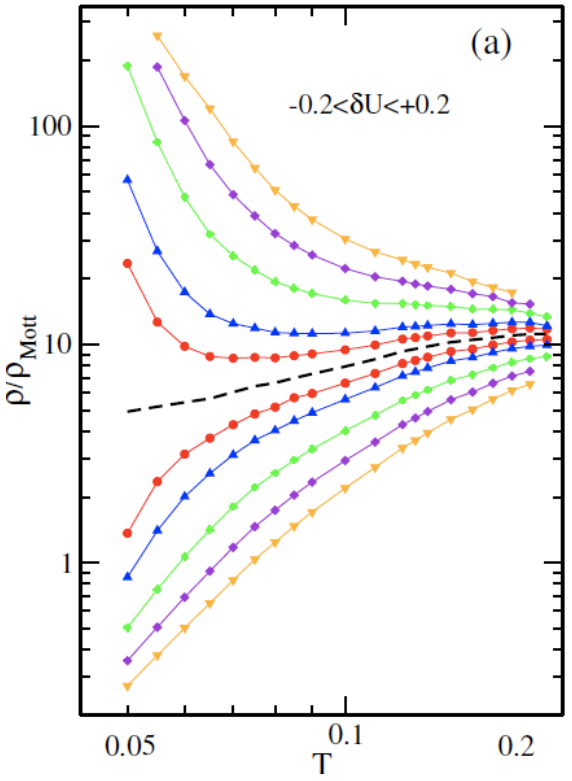
Crossover - *"quantum Widom line"* !

Recent work: Sordi, Tramblay, 2012, etc.

DMFT theory

around Widom line





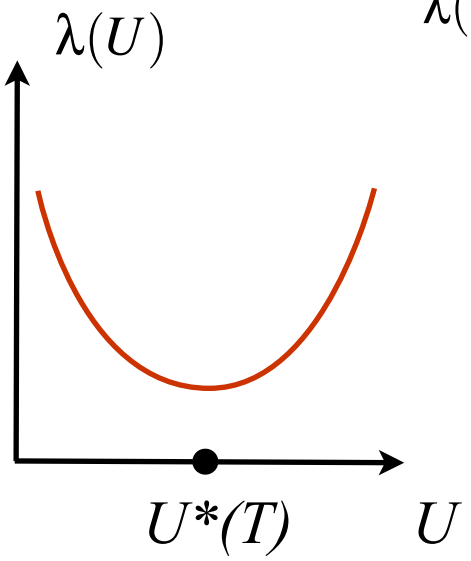
kFl << 1
"impossible"

kFl = 1

MOSFET: Tc ~2%TF ~ 200mK

Crossover line: eigenvalue analysis

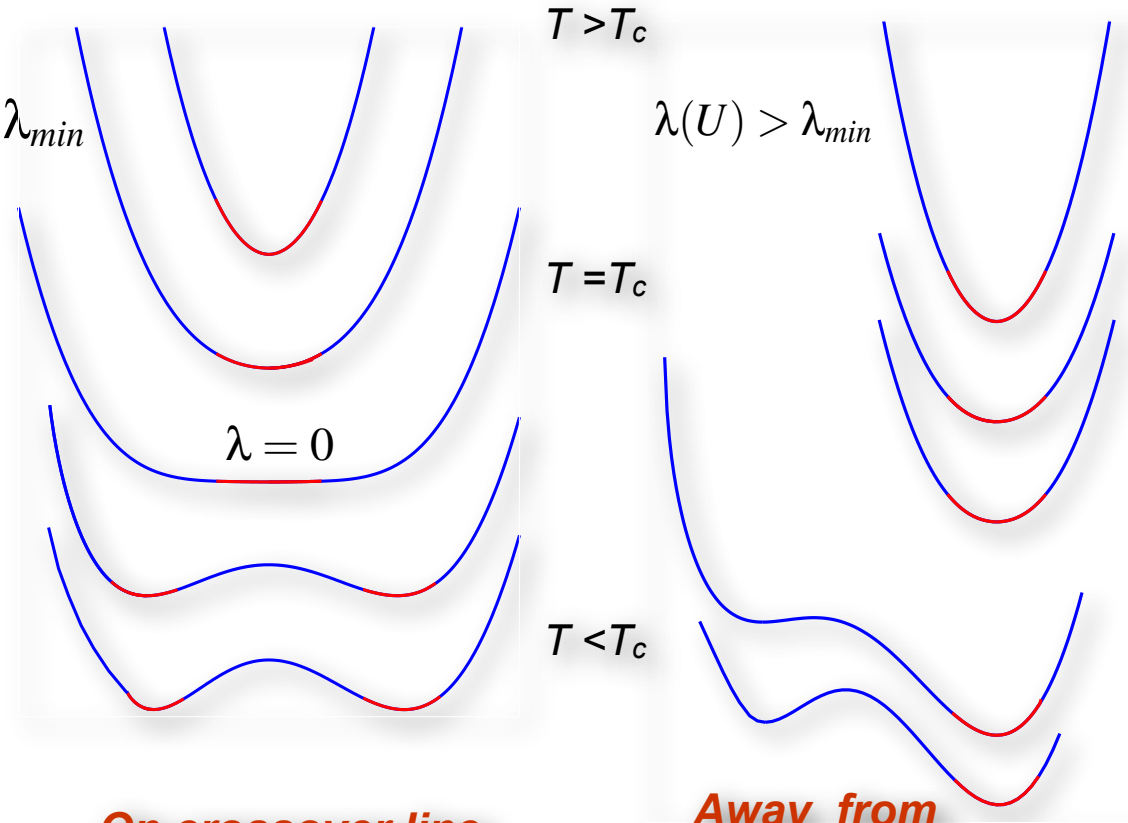
Curvature - eigenvalue



$$\delta U = U - U^*(T)$$

Free energy landscape

(actual quantitative results!)



On crossover line

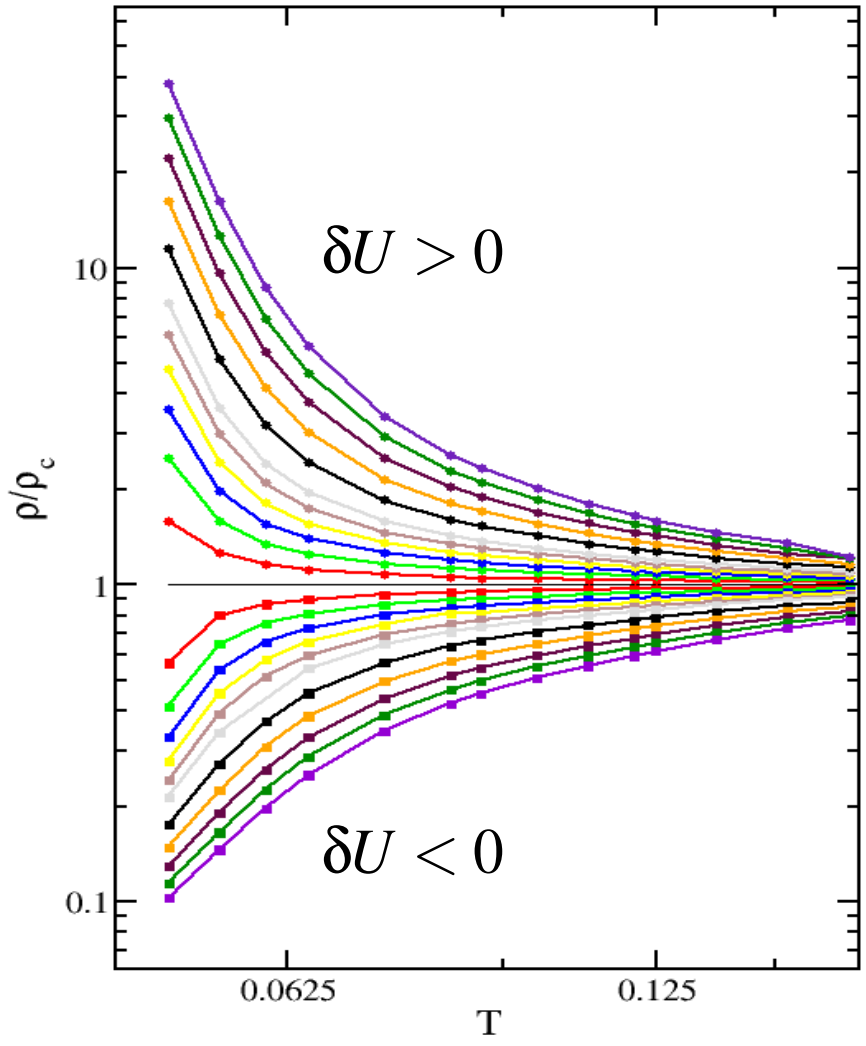
$$\delta U(T) = 0$$

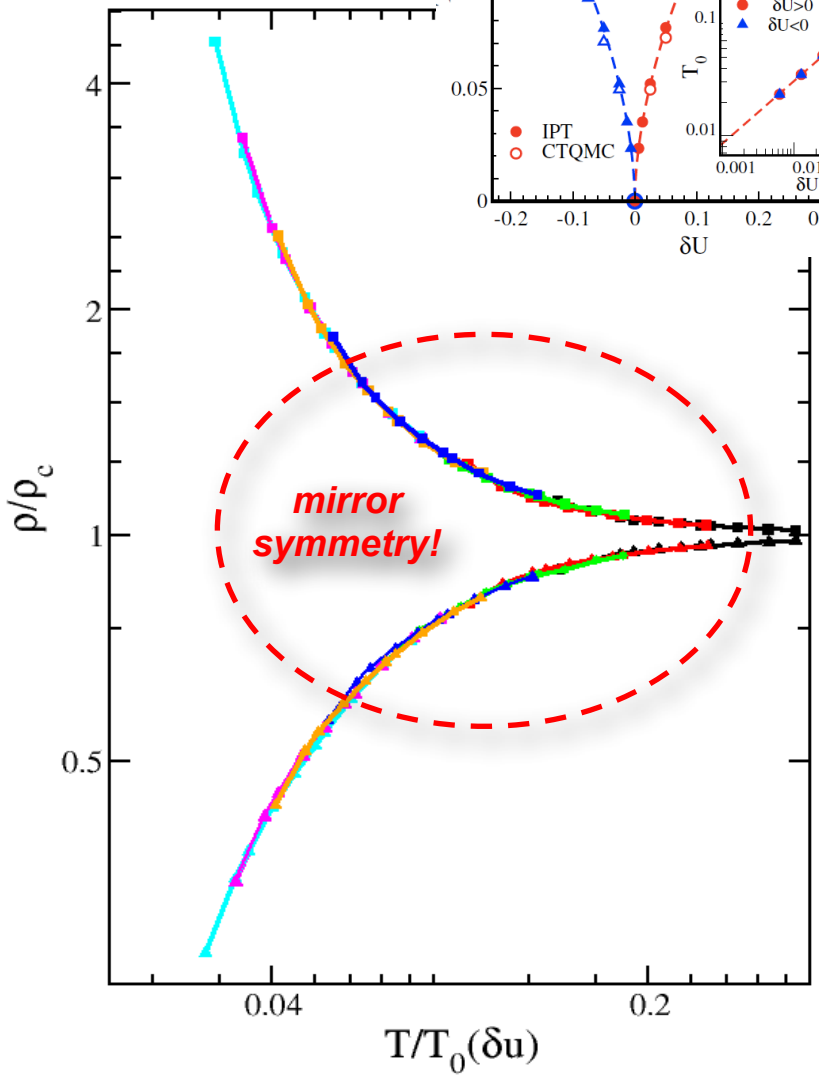
Away from crossover line

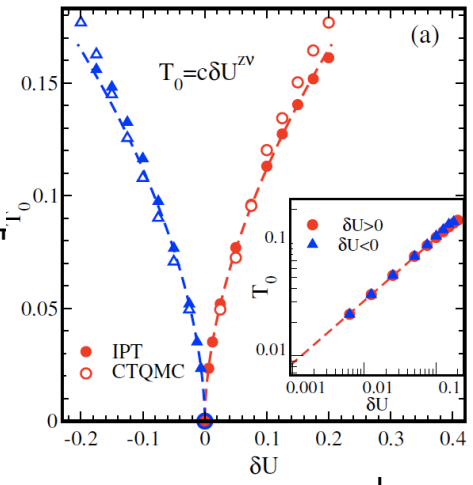
$$\delta U(T) \neq 0$$

Scaling

$$\rho(\delta U, T)/\rho_c(T) = f(T/T_o(\delta U))$$

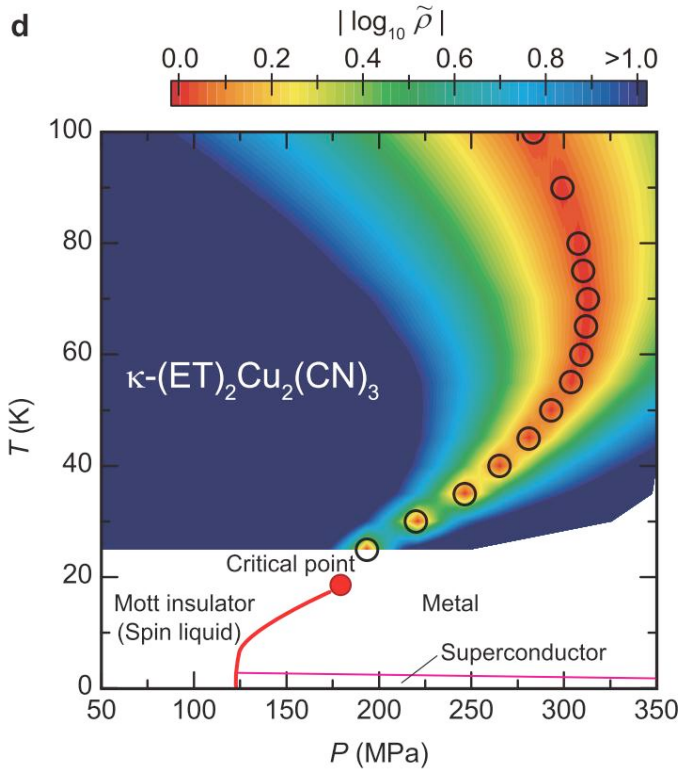




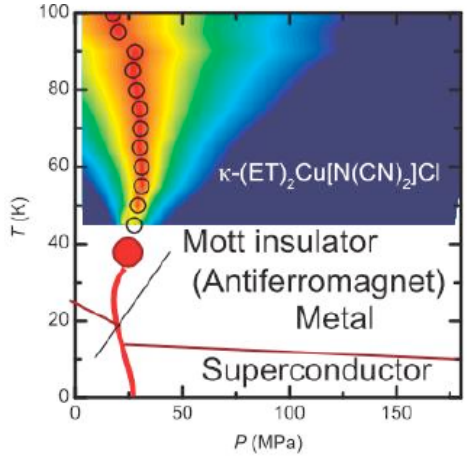


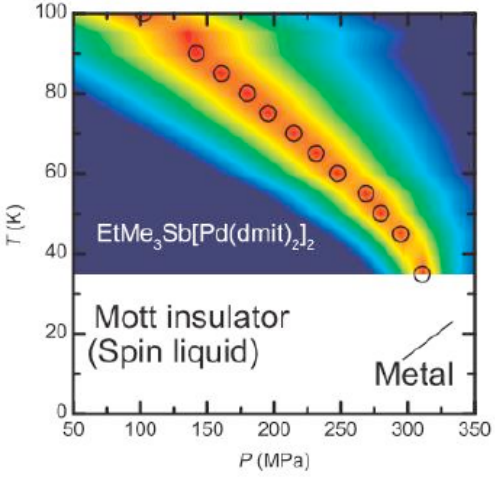
Mott organics: universal high-T scaling

K. Kanoda et al., Nature Physics (2015)



Strong frustration:
spin liquid at low T

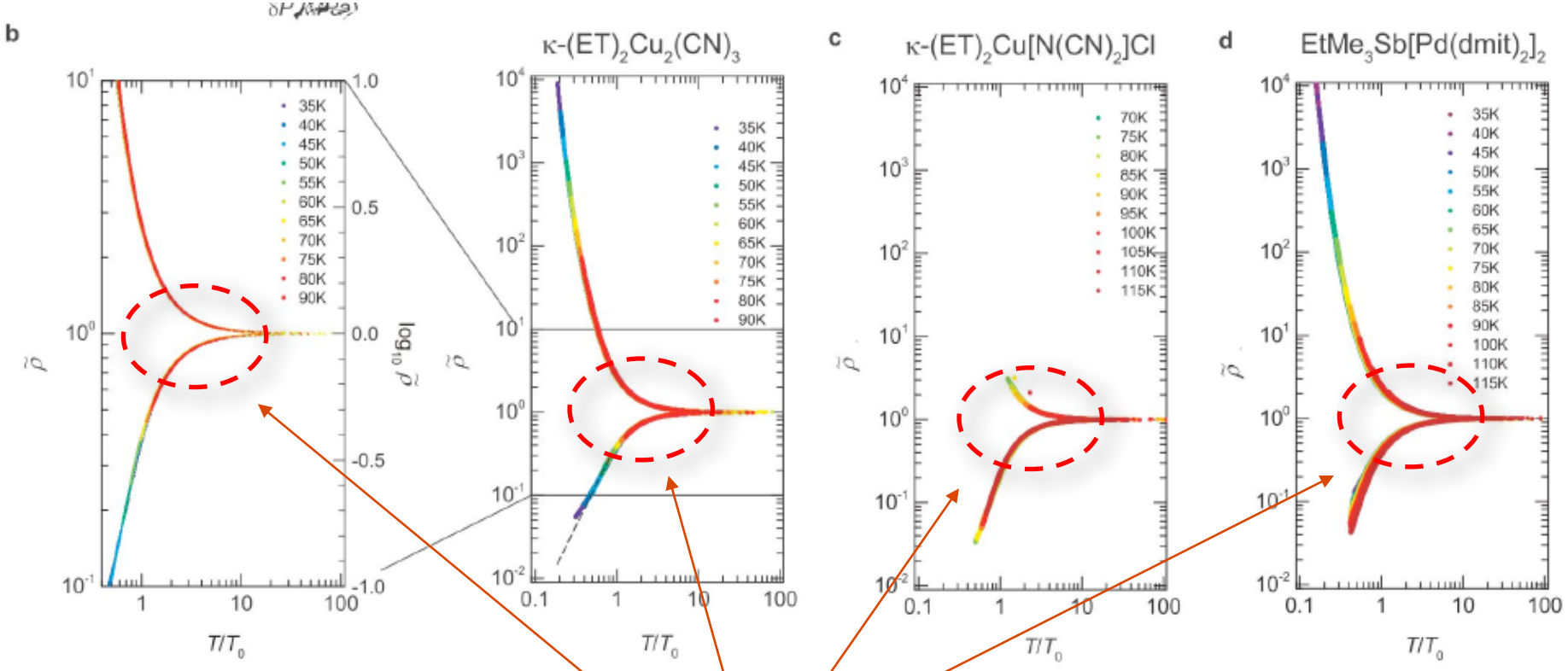




Weaker frustration:
AFM at low T

Mott organics: universal high-T scaling

K. Kanoda et al., Nature Physics (2015)



zv = 0.60 and c = 25.3 for κ-$Cu_2(CN)_3$

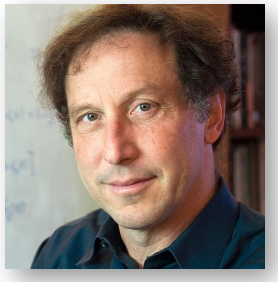
zv = 0.55 and c = 65.8 for κ-Cl

zv = 0.65 and c = 18.9 for $EtMe_3Sb$-dmit

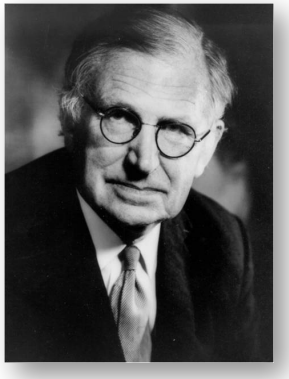
mirror symmetry!

$$\tilde{\rho} = \exp[\pm(T/T_0)^{-1/z_\nu}]$$

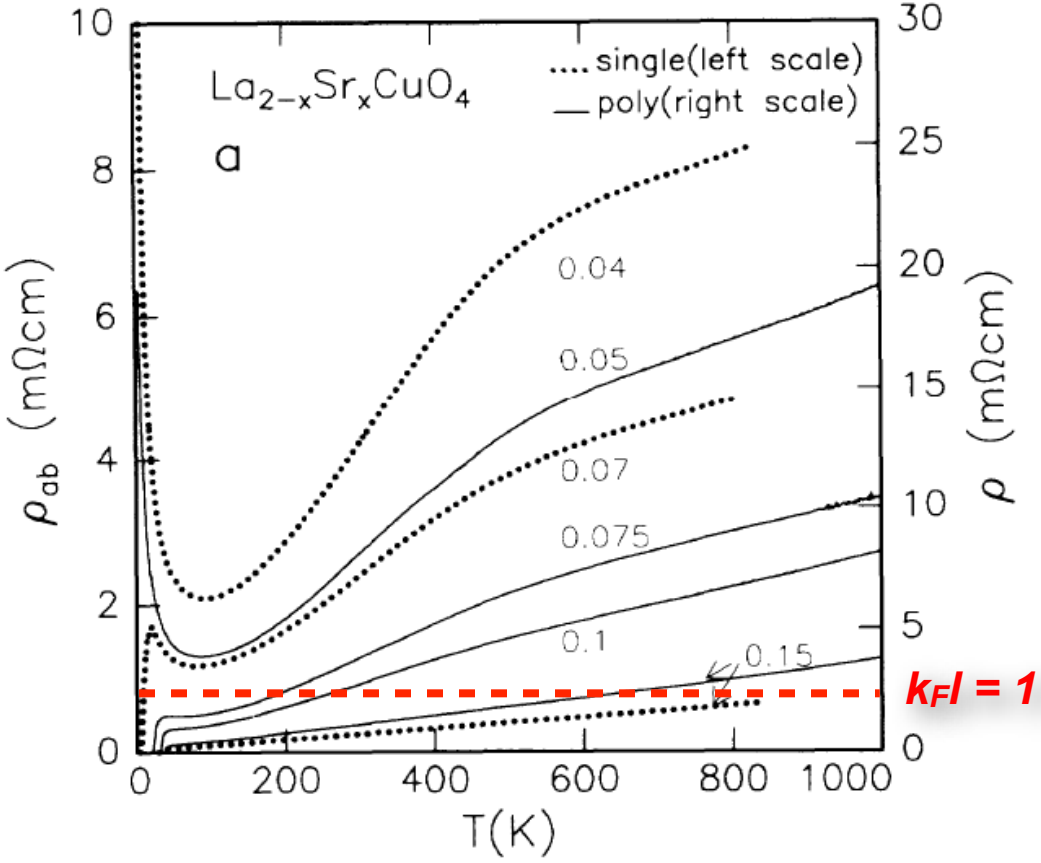
"stretched exponential"



Doped Mott insulators:
Bad Metals vs. Quantum Criticality??

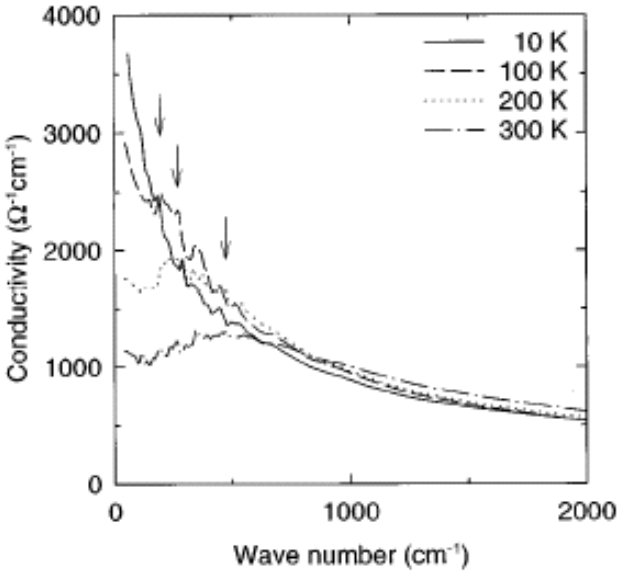


Mott-Ioffe-Regel limit: $k_F l > 1$



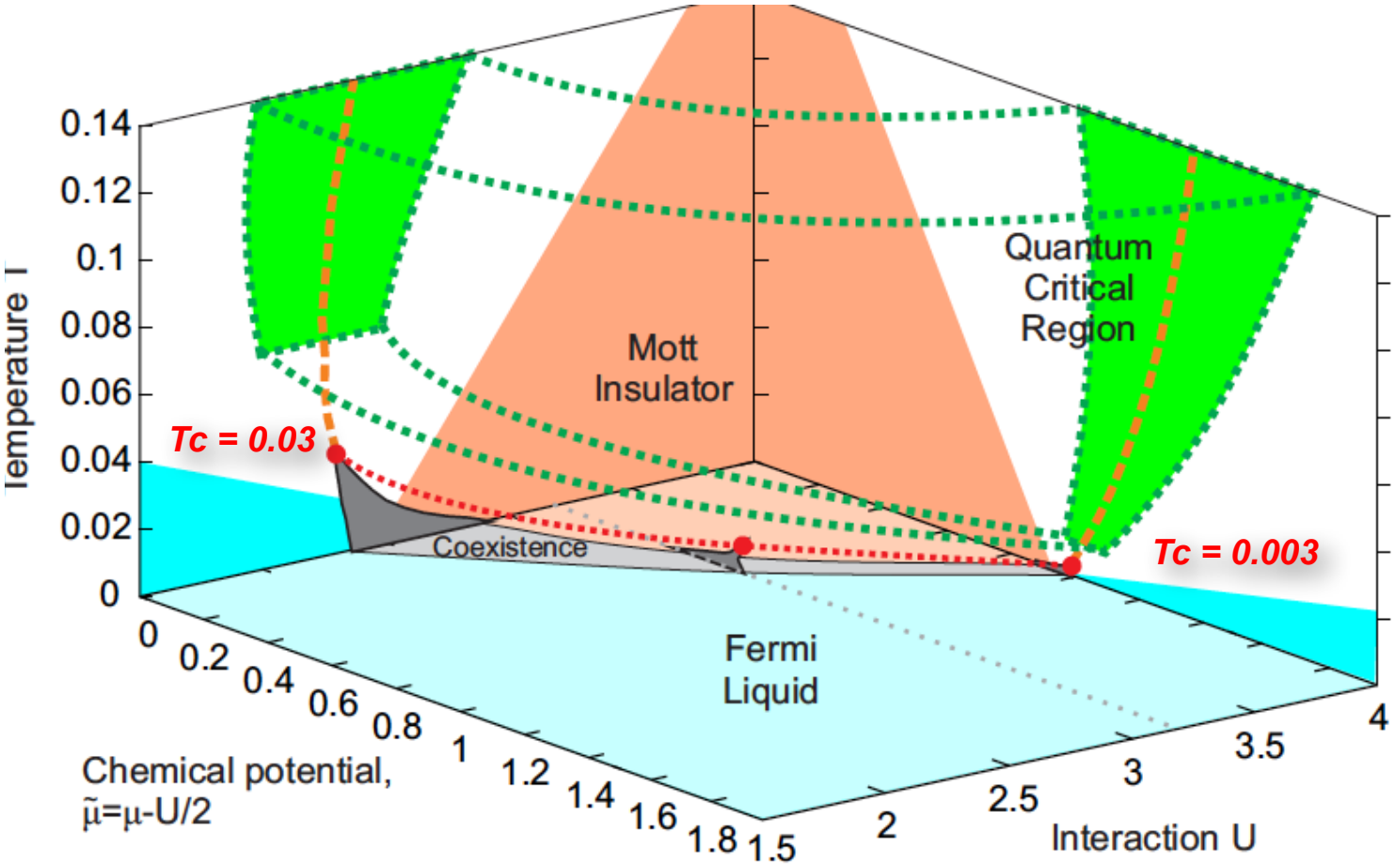
$k_F l = 1$

Experiment: **H. Takagi, 1992**



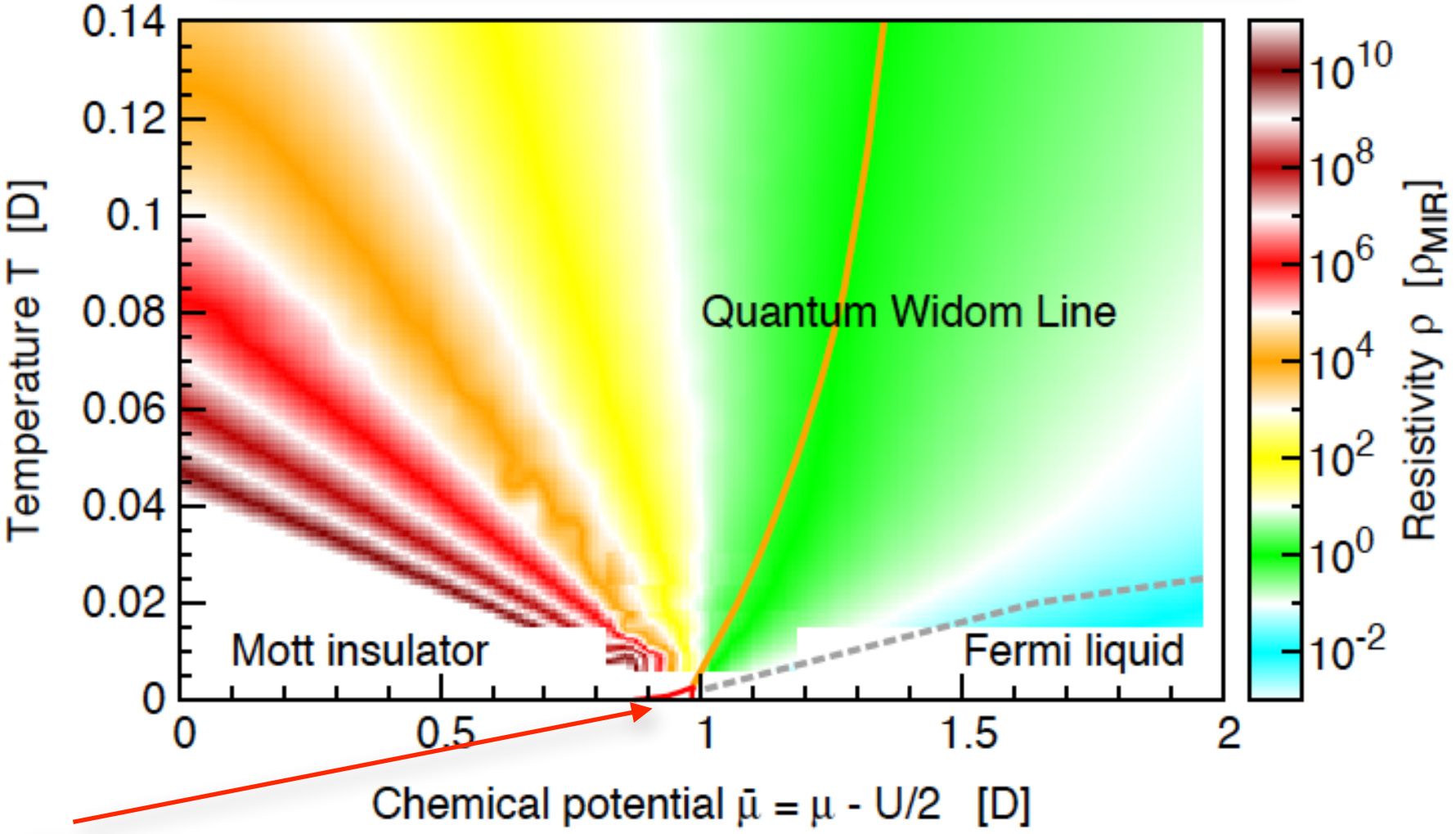
Bad-Metal Behavior Reveals Mott Quantum Criticality in Doped Hubbard Models

J. Vučičević,[1] D. Tanasković,[1] M. J. Rozenberg,[2] and V. Dobrosavljević[3]



Doped Mott: DMFT vs. QCP?

J. Vučičevic, D.Tanaskovic, M. Rozenberg, and V. D., PRL 2015

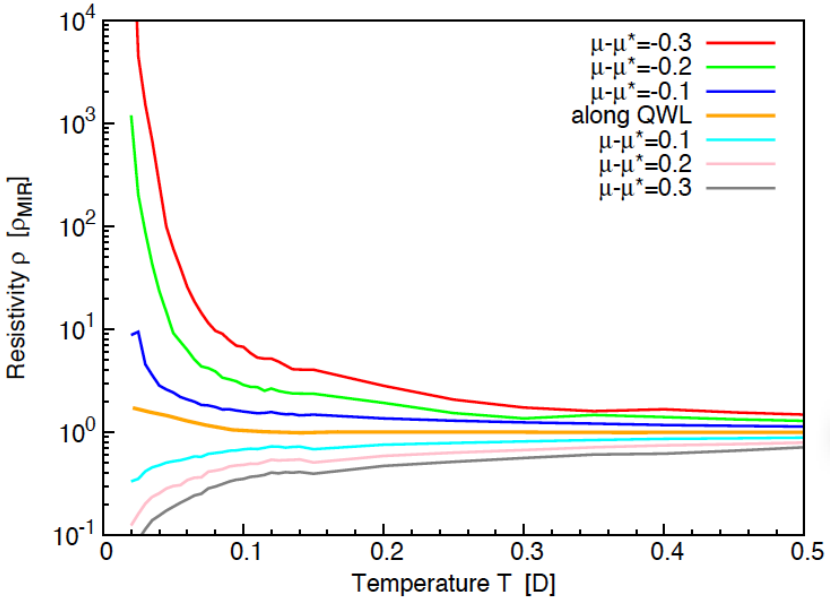


TINY coexistence dome

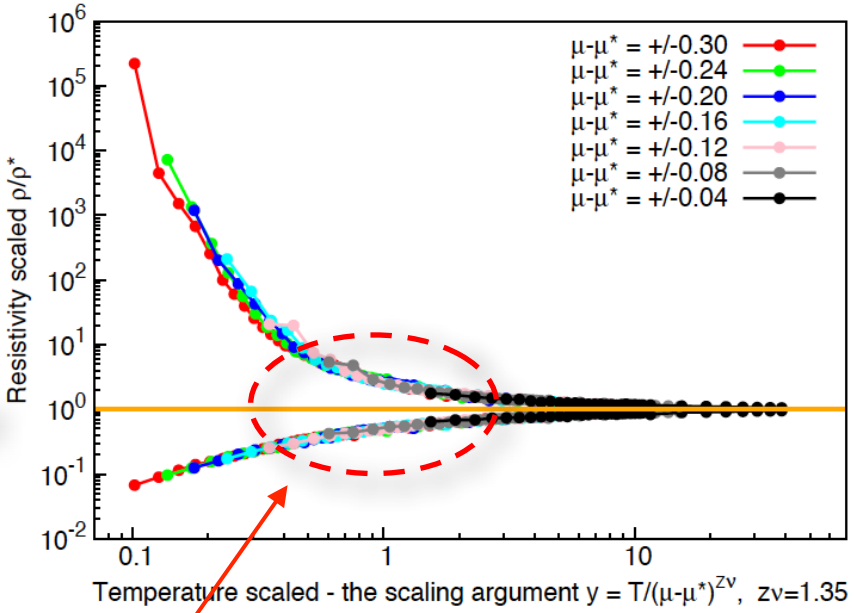
Tc = 0.003

Doped Mott:QC Scaling

J. Vučičevic, D.Tanaskovic, M. Rozenberg, and V. D., PRL 2015



$k_F l = 1$



mirror symmetry:
defines QC region

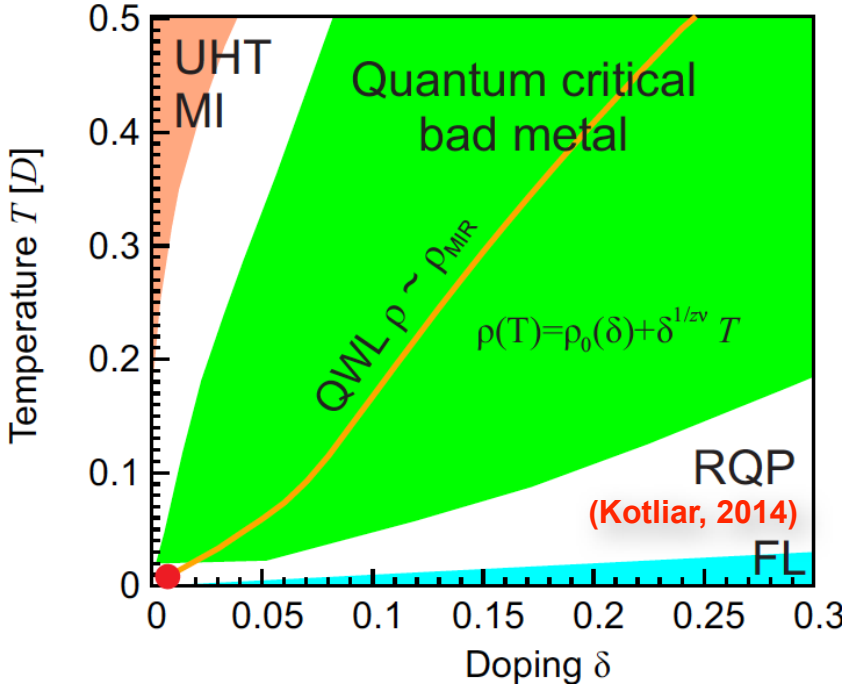
New feature:
Quantum Widom Line - MIR limit

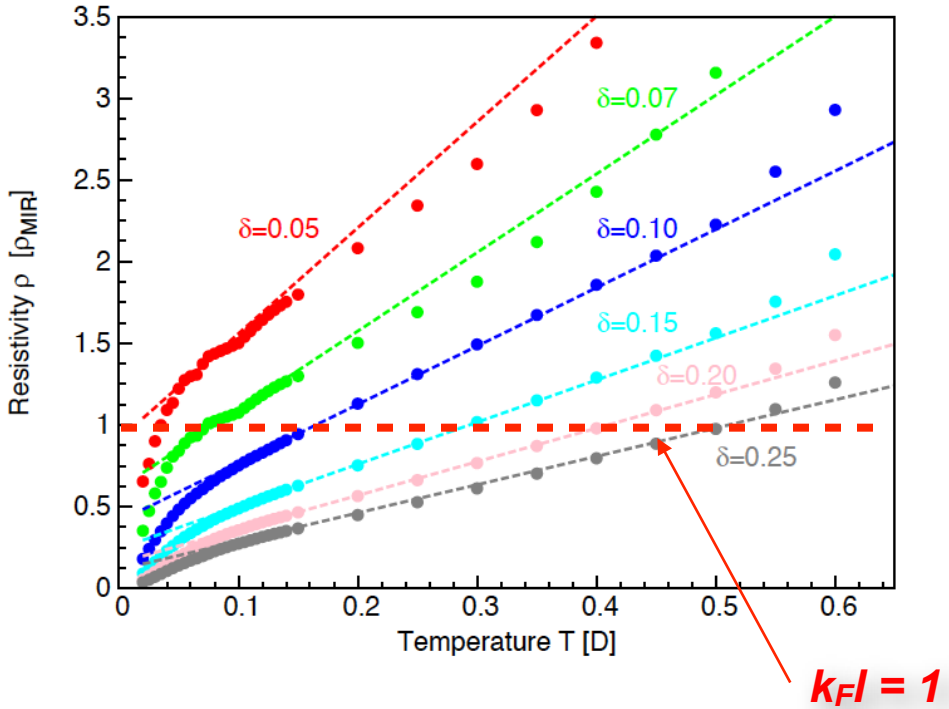
$$\rho(T,\mu) = \rho^* \exp\{A(\mu - \mu^*(T))/T^{\nu z}\}$$

"stretched exponential"

Doped Mott: Quantum Critical Region?

J. Vučičevic, D.Tanaskovic, M. Rozenberg, and V. D., PRL 2015





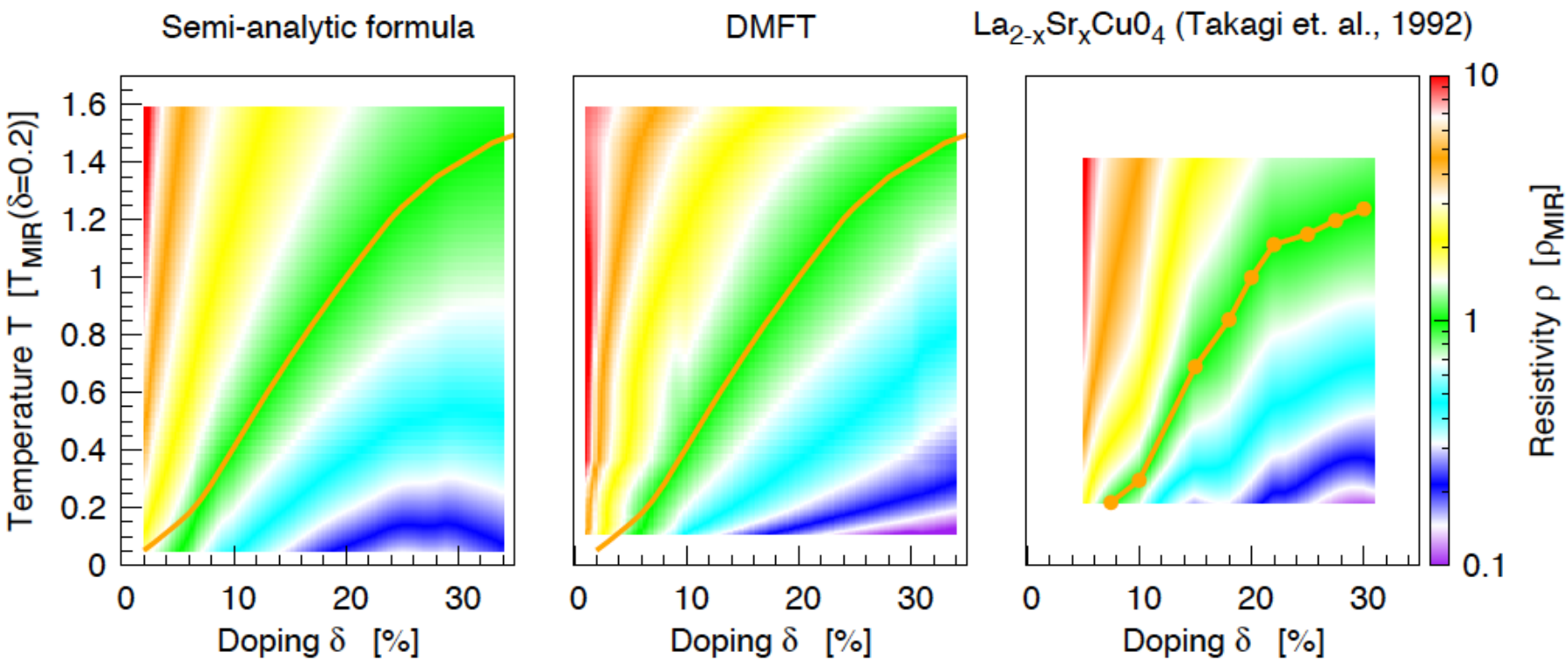
Key Results:

Bad Metal (linear resistivity ~ MIR limit) = Mott QC region

QC Scaling - (semi) analytical formula for linear-T resistivity

Doped Mott: Theory vs. Experiment

J. Vučičevic, D.Tanaskovic, M. Rozenberg, and V. D., PRL 2015



Mott QC region: universal behavior at high temperatures

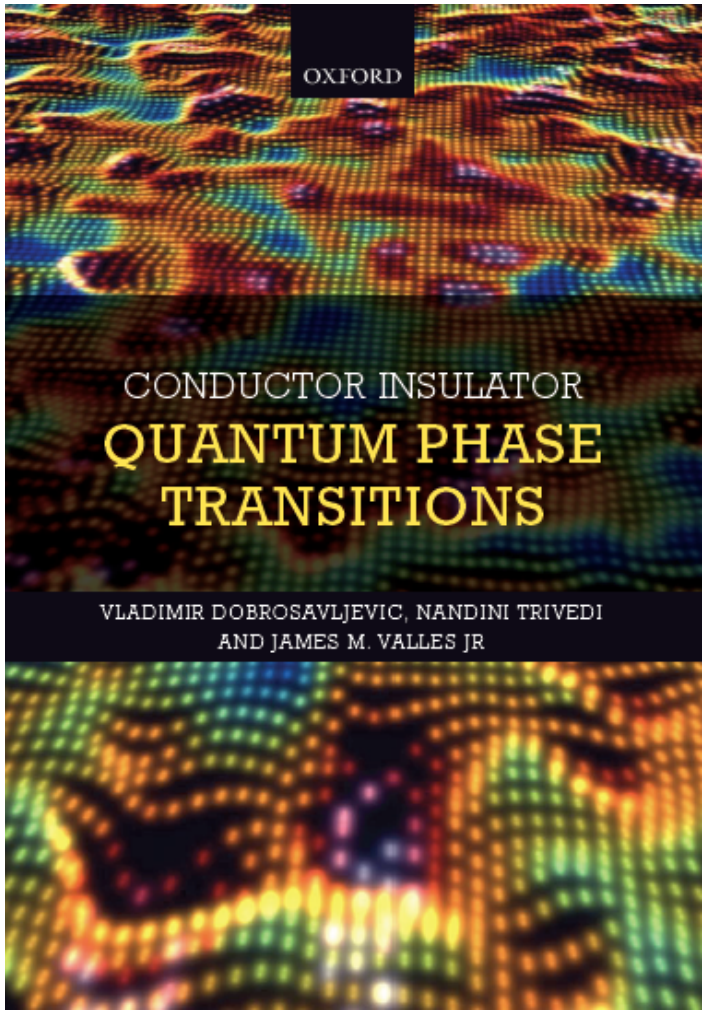
Moral of the story

- using words anyone can understand -

Bad Liquid:
AdS-CFT??

Viscous (quantum) liquid is not a gas (Landau quasiparticles)

To learn more:



http://badmetals.magnet.fsu.edu

(just Google "Bad Metals")

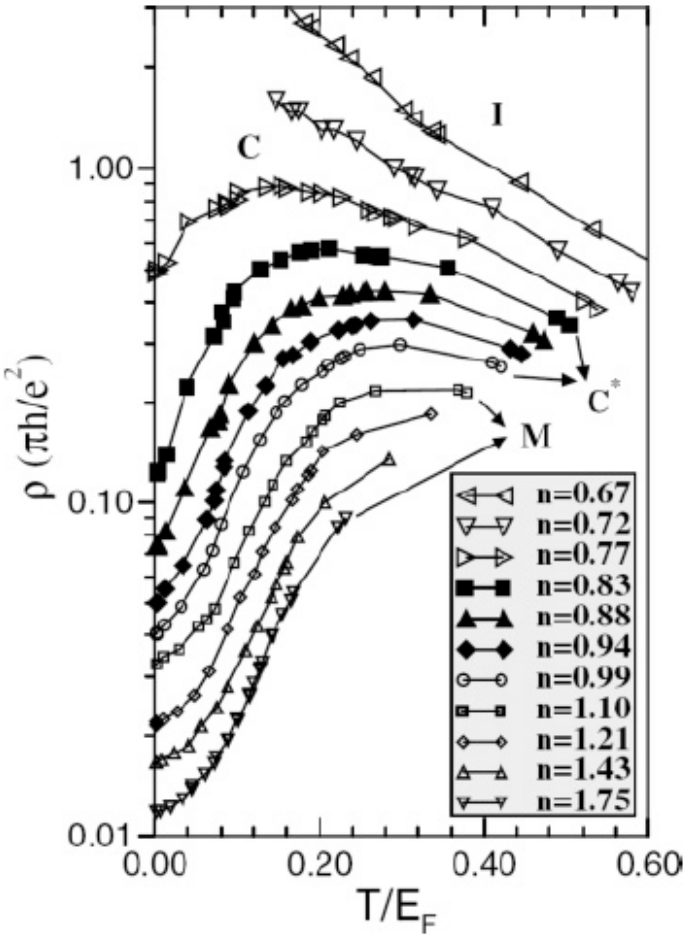
Book:

Oxford University Press, 2012

ISBN 9780199592593

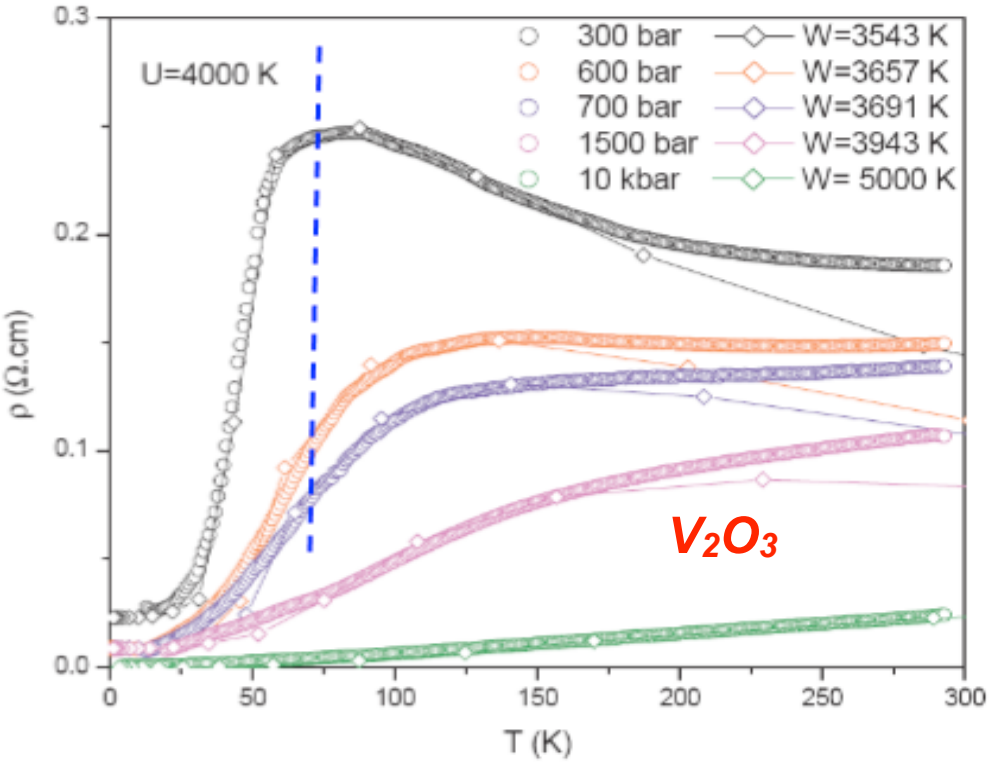
Really, but really bad metals: resistivity maxima (experiments)

MOSFETs



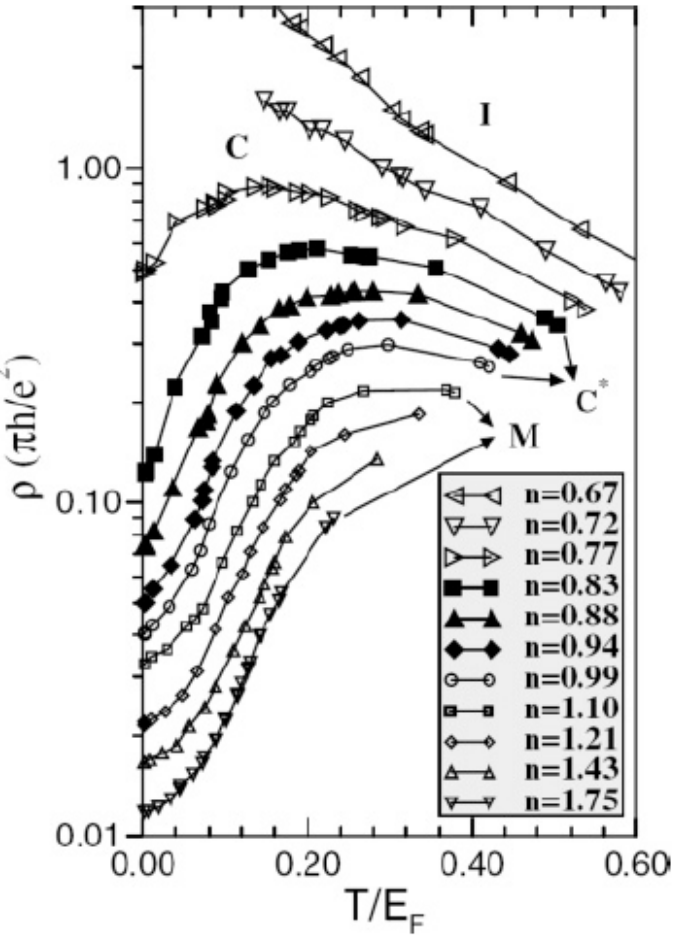
And now...

something completely different



Phenomenological scaling (experiments)

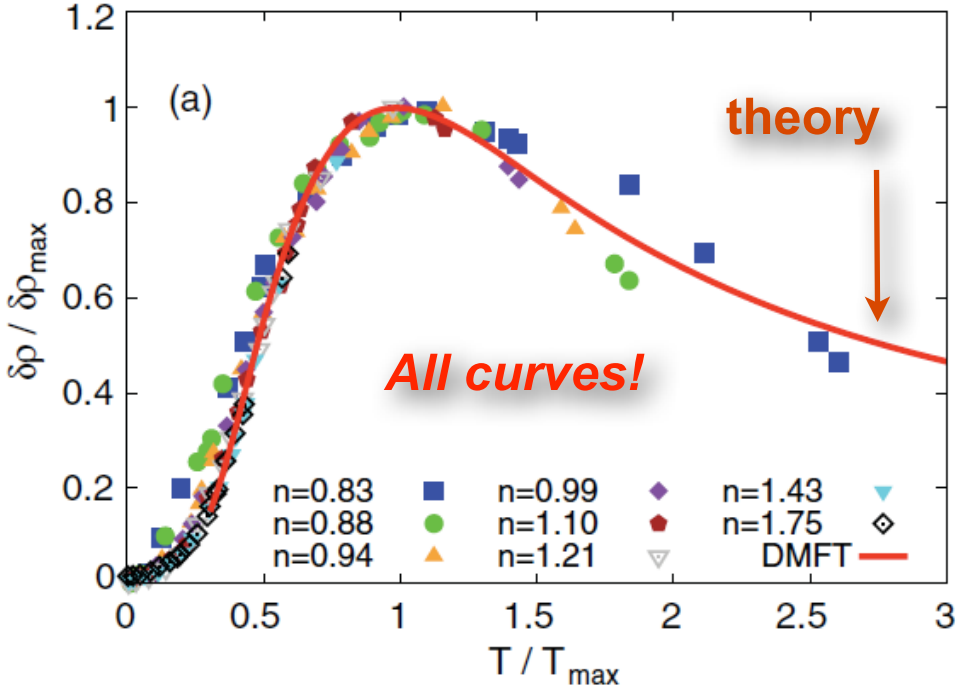
MOSFETs



$$\rho(T) = \rho_o + \delta\rho(T)$$

$$\delta\rho(T) = \delta\rho_{\max} f(T/T_{\max})$$

$$\delta\rho_{\max} = \rho_{\max} - \rho_o$$

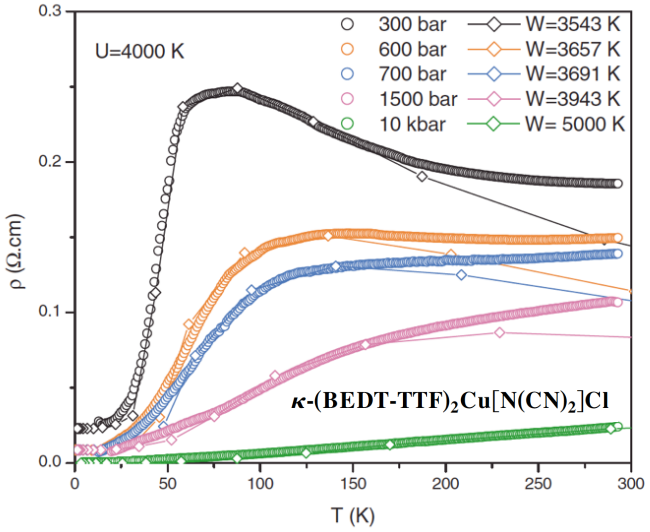


Evaporating the Fermi liquid

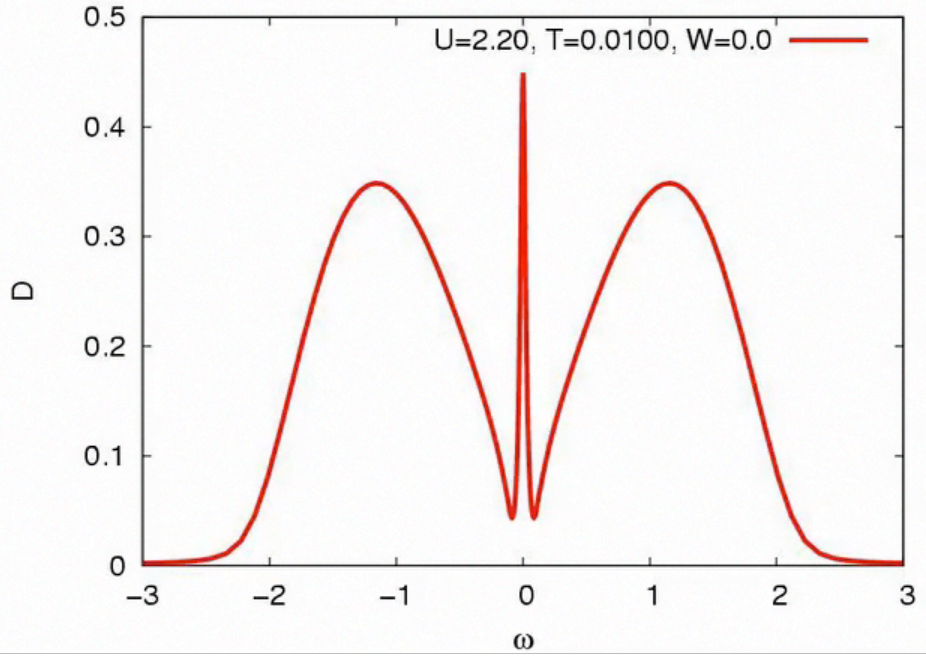
Darko Tanaskovich

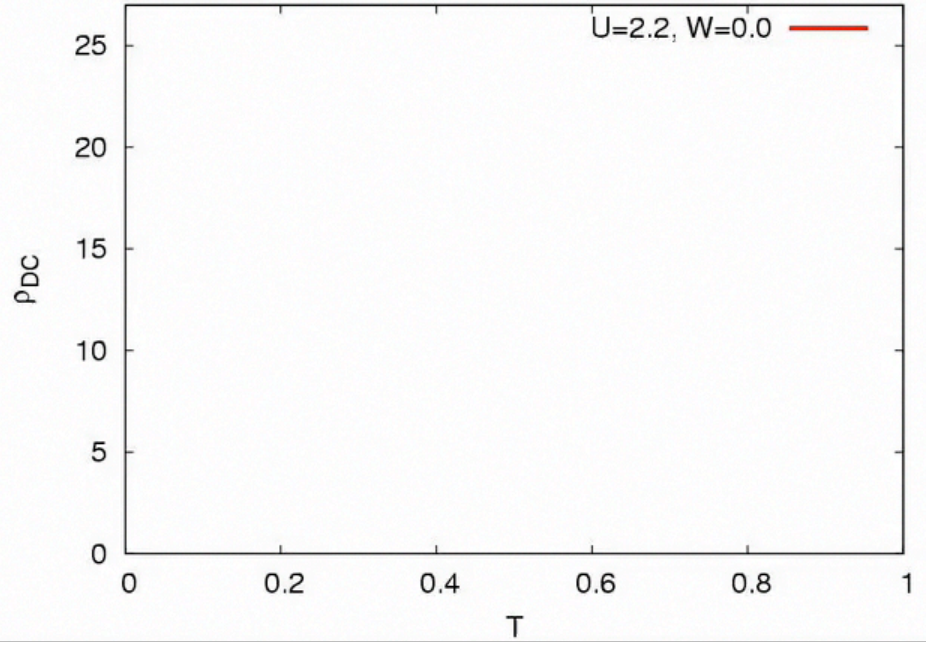
Low Fermi liquid coherence scale

$$T_{FL}^{*} \sim ZT_F \sim T_F/m^{*}$$



Thermal death of quasi-particles?



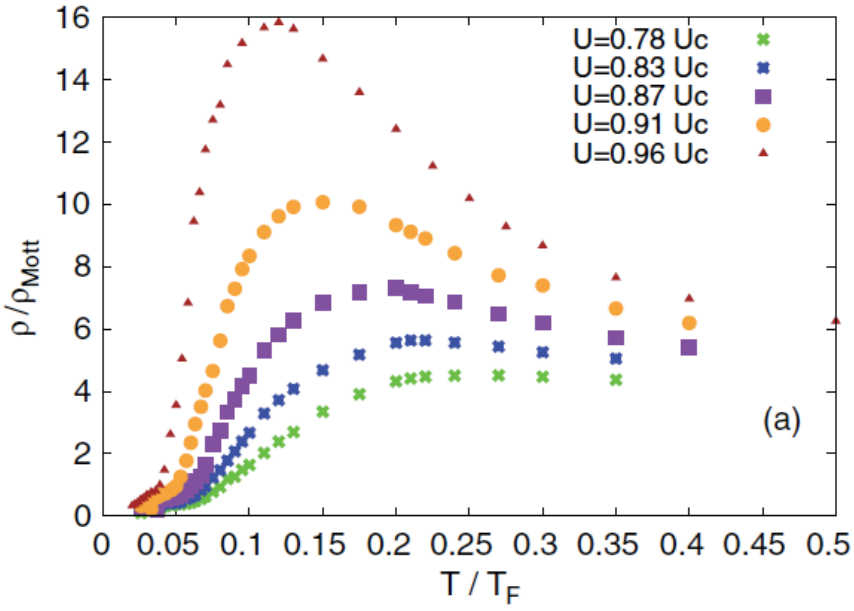


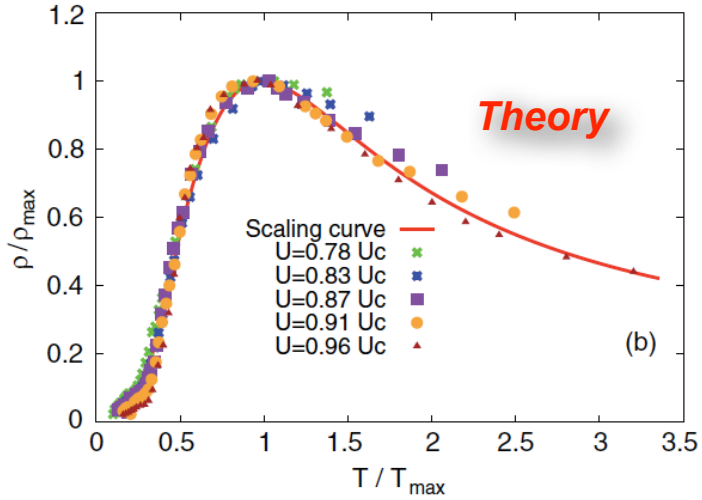
PHYSICAL REVIEW B **85**, 085133 (2012)

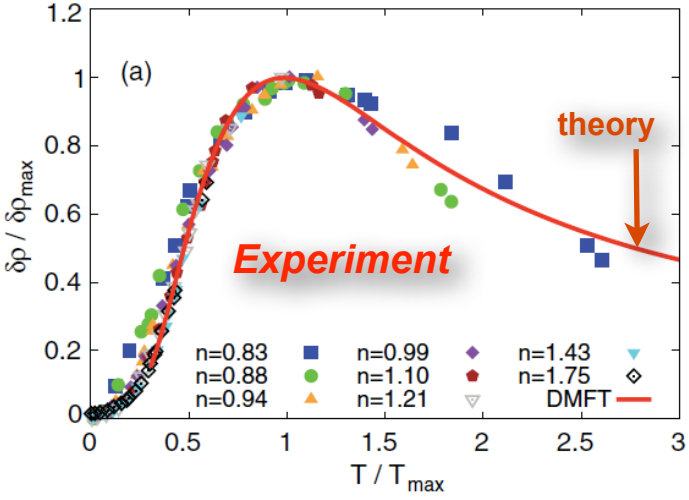
Wigner-Mott scaling of transport near the two-dimensional metal-insulator transition

M. M. Radonjić,[1] D. Tanasković,[1] V. Dobrosavljević,[2] K. Haule,[3] and G. Kotliar[3]

DMFT theory

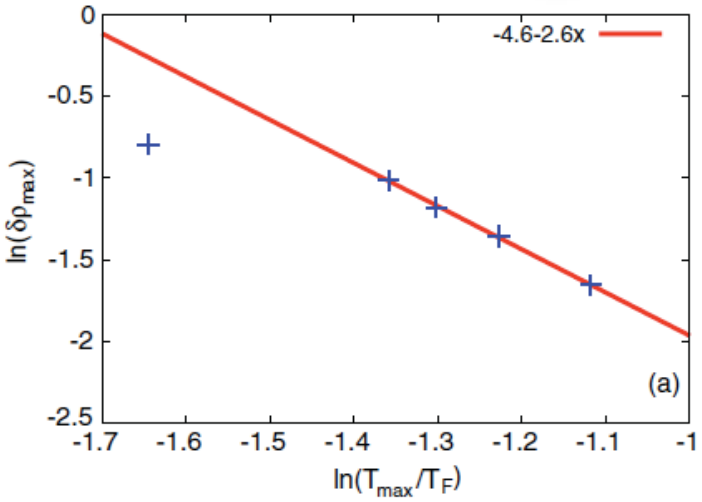


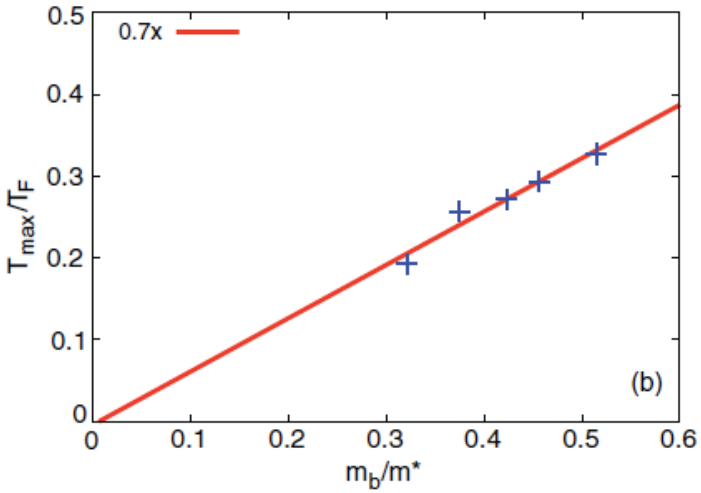
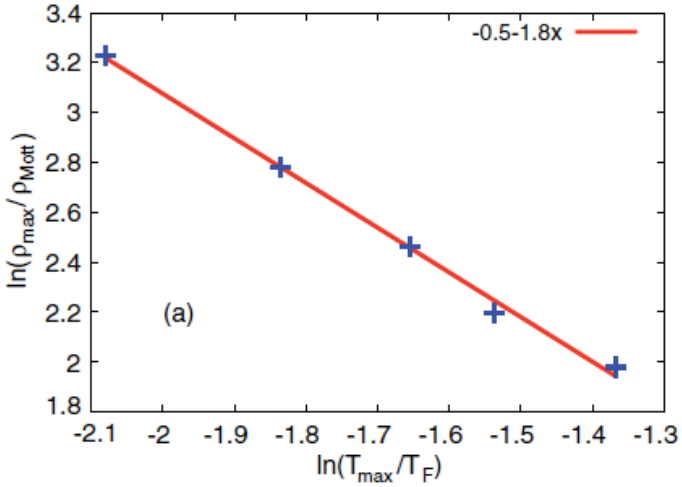
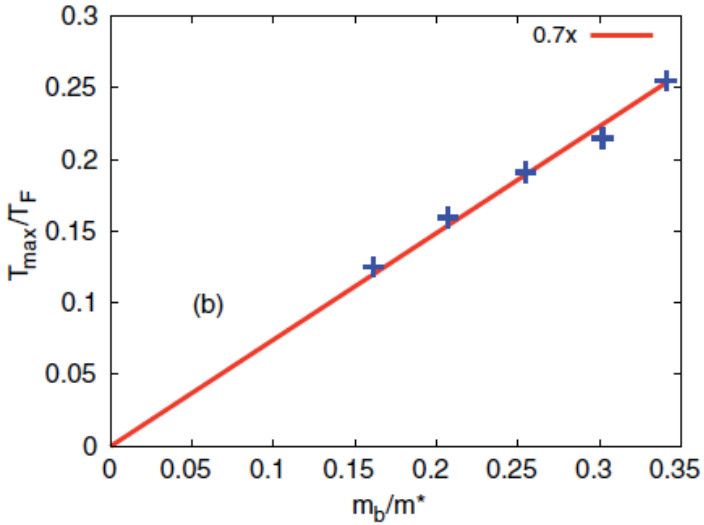




Approaching the transition - trends

DMFT Theory





Experiments